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- Styles of Programming
 - Imperative Programming:
 - Describe in detail how computation proceeds
 - Basically, change states of variables
 - This is what we practiced up till now

- Functional Programming
 - Define functions
 - Specify program behavior by executing nested functions
 - Pure functional programming: No variables that capture a state
 - Advantage: Easier to prove programming correctness

- Declarative Programming
 - Specify what a program should do
 - System figures out how to do it.
 - Example 1: Prolog (Classic AI programming language)
 - Specify rules in Prolog:
 - animal(X) :- cat(X) means every cat is an animal
 - ?- cat(tom). means that tom is a cat
 - You can ask about the world defined by these rules
 - ?- animal(X). asks for what things are animals
 - Prolog consists of rules and base facts, then on its own finds out other facts.

- Declarative Programming:
 - Example 2: SQL Database Language
 - Database consists of relations stored in various tables
 - Example:

Marquette_ID	First_Name	Family_Name	Address
123123007	David	Roy	1984 31st Street, Milwaukee, WI 54321
97007007	Thomas	Schwarz	4821 Wisconsin Ave, Milwaukee, WI 54213
14309873	Joseph	Cuelho	9821 12th Avenue, Milwaukee, WI 54321
90874132	Donald	Drumpf	321 Pennsylvania Ave, Madison, WI 32451

- Declarative Programming:
 - Example SQL:
 - SQL statement describes all combinations of record pieces

```
SELECT first_name, family_name FROM addresses, classes

WHERE classes.name = "COSC1010" and classes.role = "instructor" and classes.id = addresses.id
```

- Declarative Programming:
 - Example SQL:
 - SQL statement describes all combinations of record pieces
 - How the database engine performs the query is not specified
 - In fact, for complicated queries, the database will try out several ways before selecting the actual algorithms

- Object-Oriented Programming
 - Program defined various objects
 - Objects have data and methods
 - E.g. Marquette Persons have IDs, names, addresses, ...
 - Classes have lists of participants
 - We will learn Object-Oriented (OO) programming in this class

- Recall anonymous functions
 - We can define a function with the lambda expression
 - Example:

```
lambda x, y: (x+y)/(x**2+y**2+1)
```

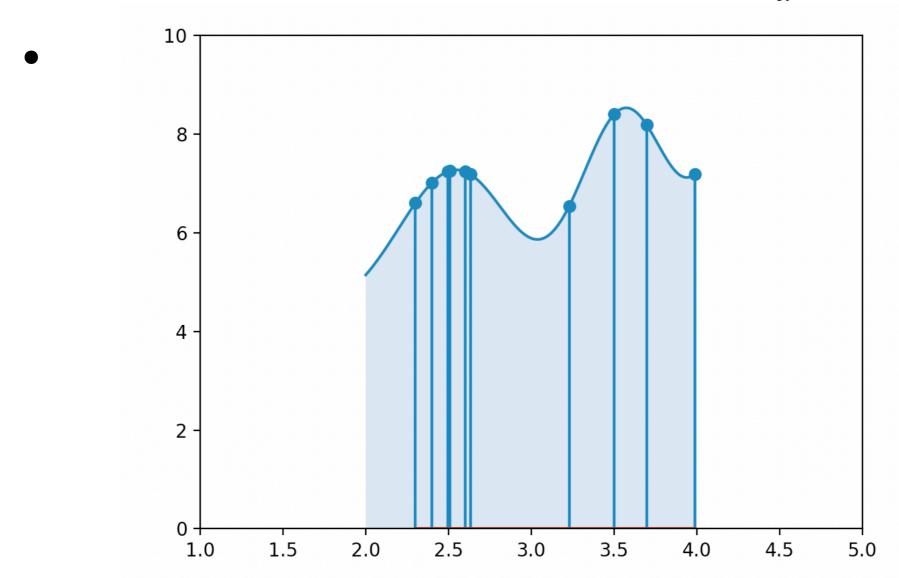
creates a function without name

```
def fun(x,y):
return (x+y)/(x**2+y**2+1)
```

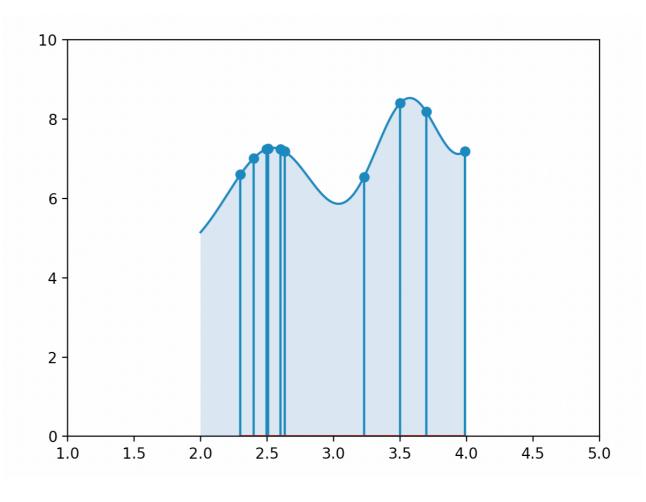
creates the same function with a name

- Python can use functions as arguments in functions
- Python can use functions as return values

• Monte Carlo Integration of a function: $\int_{a}^{b} f(x)dx$



- Idea: Select n random points between a and b
- Calculate the function value on these points
- Calculate their average
- Multiply with (b-a)
- This is an estimate
 - for the integral



Implementation

```
import random as rd

def integral(fun, a, b, nr_of_points):
    sum_of_f = 0
    for _ in range(nr_of_points):
        sum_of_f += fun(rd.uniform(a,b))
    mean_of_fs = sum_of_f/nr_of_points
    return mean of fs * (b-a)
```

Implementation

```
import random as rd

def integral(fun, a, b, nr_of_points):
    sum_of_f = 0
    for _ in range(nr_of_points):
        sum_of_f += fun(rd.uniform(a,b))
    mean_of_fs = sum_of_f/nr_of_points
    return mean_of_fs * (b-a)
```

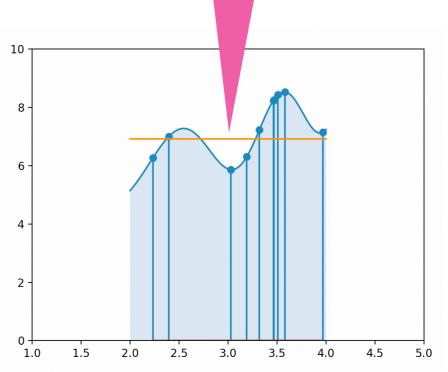
Contains now $f(r_1) + f(r_2) + \dots + f(r_n)$

Implementation

```
import random as rd

def integral(fun, a, b, nr_of_points):
    sum_of_f = 0
    for _ in range(nr_of_points):
        sum_of_f += fun(rd.uniform(a,b))
    mean_of_fs = sum_of_f/nr_of_points
    return mean_of_fs * (b-a)
```

Contains now average function value (estimated)



2

1.0

1.5

2.0

2.5

3.0

3.5

4.0

4.5

5.0

```
import random as rd
def integral (fun, a, b, nr of points):
    sum of f = 0
    for in range(nr of points):
        sum of f += fun(rd.uniform(a,b))
    mean of fs = sum of f/nr of points
    return mean of fs * (b-a)
                                  8
                                  6
```

Area is same as the one enclosed by the red lines

We can try this out using a lambda expression

```
for in range (20):
    print(integral(lambda x: 5+x**2/5+math.cos(x**2),2,4,1000))
                             13.848738547694959
                             13.84527895244639
                             14.017133065965641
                             13.832408510459572
                             13.873003112163618
                             13.75656692127387
                             13.87544139865498
                             13.807364056962463
                             13.819856780953849
                             13.785217661244614
                             13.782351635543083
                             13.818585721154232
                             13.842831044731115
```

13.853038466753764

13.832754911335963

- Returning a function
 - Calculate a random polynomial of degree 3
 - Idea:
 - generate four "random" coefficients
 - create the polynomial
 - return it

Implementation

```
import random as rd

def random_poly():
    a = rd.randint(-3,3)
    b = rd.randint(-5,5)
    c = rd.randint(-5,5)
    d = rd.randint(-2,2)
    return lambda x: a*x**3+b*x**2+c*x+d
```

Implementation without using lambda

```
def random_poly_d():
    a = rd.randint(-3,3)
    b = rd.randint(-5,5)
    c = rd.randint(-5,5)
    d = rd.randint(-2,2)
    def inner(x):
        return a*x**3+b*x**2+c*x+d
    return inner
Create a new function
```

Implementation without using lambda

```
def random_poly_d():
    a = rd.randint(-3,3)
    b = rd.randint(-5,5)
    c = rd.randint(-5,5)
    d = rd.randint(-2,2)
    def inner(x):
        return a*x**3+b**.**2+c*x+d
    return inner
```