Repetition

- The foo-bang problem
 - Print a list of all numbers between 1 and 100
 - Whenever the number is divisible by 3, print "foo" afterwards
 - Whenever the number is divisible by 5, print "bang"
 - If both conditions are set, print "foo-bang"
- This is a version of a well-known easy programming interview question

```
def foo_bang(n):
    for i in range(1, n+1):
        if i%3 == 0 and i%5 == 0:
            print(i, 'foobang')
        elif i%3 == 0 and i%5 != 0:
            print(i, 'foo')
        elif i%3 != 0 and i%5 == 0:
            print(i, 'bang')
        elif i%3 != 0 and i%5 != 0:
            print(i)
        else:
            print(f'With {i}: Logic error in program')
```

- A use case for continue
 - Find all numbers x between 1 and 10000 that satisfy the following conditions simultaneously:
 - x is not a square
 - $x^3 + 2$ is divisible by 4
 - (x-1)(x+1) is not divisible by 7
 - (x+2)(x+3) is divisible by 5

Find the smallest number
$$n$$
 such that $\sum_{i=1}^{n} \frac{1}{i^2} > \sqrt{2} + \frac{1}{10}$

- Each letter stands for a different digit.
 - Solve:

•

SEND +MORE

MONEY

- Each letter stands for a different digit
 - Solve

```
six
+ six
+ six
=
nine
+nine
```

• Solve:

```
nine
+seven
+seven
+seven
```

thirty

Classes and Object 1

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Classes and Objects

- Imperative programming manipulates the state of memory
 - Breaks up tasks through procedures and functions
- Object Oriented Programming
 - Creates objects that interact with each other
 - Objects are defined with a user-defined data type

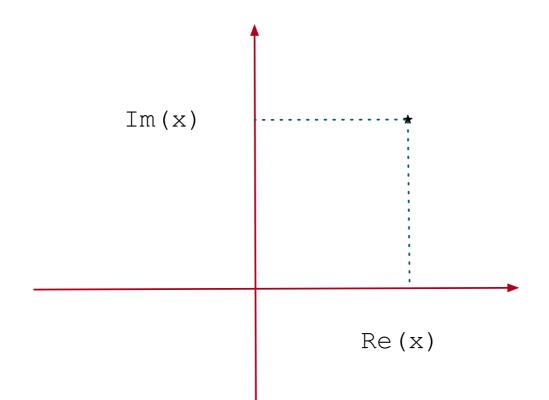
Classes and Objects

- Each object maintains its own state
 - Objects manipulate themselves and other objects through methods

Classes and Objects

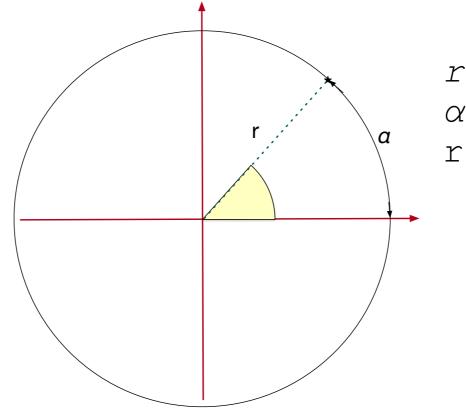
- Running Example:
 - Complex Numbers
 - Complex numbers live in the complex plane
 - Two canonical way of representing them:
 - Via coordinates (the real and the imaginary part)
 - Via length and angle to x-axis

Complex Numbers



- Complex numbers are points in the Gaussian plane
- Can be represented as pairs (a,b)
 - a is called the real part, b is called the imaginary part
 - Written as a+ib, the "algebraic notation"

Complex Numbers



r is the length α is the phase in radians

- Polar form
 - Given by angle α with x-axis and a length r
 - Written as $r \cdot e^{i\alpha}$



Complex Numbers

- Complex numbers allow various operations such as addition, multiplication, exponentiation,
- The have a length, a real part, and imaginary part, and a phase
- They have a transpose
- And so much more

- We define the type of an object as a class
 - Objects have fields and methods
 - Fields are like variables
 - Methods are like functions

- A complex number has two fields: the real and the imaginary part
- A method would be the calculation of the length
- Another standard method would be a string describing the number

- There are two types of fields and methods:
 - Those that belong to the class:
 - Class variables (aka Class fields), Class methods
 - And those that belong to an object
 - Object variables, Object methods

- To create an object of type class, "instantiation": we define and use an initializer called __init__()
- The initializer can have arguments.
- If we create object variables and methods, we use the (quasi-)keyword self to refer to the object.

The double underscore before and after make this a reserved method name.

```
class Complex():
    def init (self, real, imaginary):
        self.re \(\Delta\) real
        self.im = \imaginary
    def str (self):
        return "{}+i{}".format(self.re, self.im)
if name == " main
    a = Complex(-2, 3)
   b = Complex(1, 2)
   print(a, b)
```

They are called dunder methods.

The "self" is required. It renders this is an instance method

```
class Complex():
    def __init__(self, real, imaginary):
        self.re = real
        self.im = imaginary
    def __str__(self):
        return "{}+i{}".format(self.re, self.im)

if __name__ == "__main__":
    a = Complex(-2, 3)
    b = Complex(1, 2)
    print(a, b)
```

The real and imaginary are parameters

```
class Complex():
    def __init__(self, real, imaginary):
        self.re = real
        self.im = imaginary
    def __str__(self):
        return "{}+i{}".format(self.re, self.im)

if __name__ == "__main__":
    a = Complex(-2, 3)
    b = Complex(1, 2)
    print(a, b)
```

```
class Complex():
    def __init__(self, real, imaginary):
        self.re = real
        self.im = imaginary
    def __str__(self):
        return "{}+i{}".format(self.re, self.im)

if __name__ == "__main__":
    a = Complex(-2, 3)
    b = Complex(1, 2)
    print(a, b)

This is the creation of an instance of the class. "self" is hidden, -2 is real and 3 is imaginary
```

This defines an instance field called "re"

```
class Complex():
    def __init__(self, real, imaginary):
        self.re = real
        self.im = imaginary
    def __str__(self):
        return "{}+i{}".format(self.re, self.im)

if __name__ == "__main__":
    a = Complex(-2, 3)
    b = Complex(1, 2)
    print(a, b)
```

```
class Complex():
    def __init__(self, real, imaginary):
        self.re = real
        self.im = imaginary
    def __str__(self):
        return "{}+i{}".format(self.re, self.im)

if __name__ == "__main__":
    a = Complex(-2, 3)
    b = Complex(1, 2)
    print(a, b)
```

Assigning self.whatever anywhere in the definition of the class will create an instance object

```
class Complex():
    def __init__(self, real, imaginary):
        self.re = real
        self.im = imaginary
    def __str__(self):
        return "{}+i{}".format(self.re, self.im)

if __name__ == "__main__":
    a = Complex(-2, 3)
    b = Complex(1, 2)
    print(a, b)
```

The two underscores before and after denotes __str__ as a reserved name.

```
class Complex():
    def __init__(self, real, imaginary):
        self.re = real
        self.im = imaginary
    def __str__(self):
        return "{}+i{}".format(self.re, self.im)

if __name__ == "__main__":
    a = Complex(-2, 3)
    b = Complex(1, 2)
    print(a, b)
```

__str__ takes the instance and creates a string. The string should reflect the contents of the object.

```
class Complex():
    def __init__(self, real, imaginary):
        self.re = real
        self.im = imaginary
    def __str__(self):
        return "{}+i{}".format(self.re, self.im)

if __name__ == "__main__":
    a = Complex(-2, 3)
    b = Complex(1, 2)
    print(a, b)
```

```
When print is called on objects of type complex, then Python looks first for a __str__ method and then for a __repr__ method. The __repr__ method is supposed to give more details for debugging.

def __init__ (self, real, imaginary):
    self.re = real
```

```
return "{}+i{}".format(self.re, self.im)

if __name__ == "__main__":
    a = Complex(-2, 3)
    b = Complex(1, 2)
    print(a, b)
```

def str/(self):

self.im = imaginary

- Adding Methods
 - Every complex number has a length:

$$|a+bi| = \sqrt{a^2 + b^2}$$

- To create a method calculating the length:
 - We need one argument: the object (the complex number) itself
 - This argument is called self

```
class Complex():
    def init (self, real, imaginary):
        self.re = real
                                              The one argument is self
        self.im = imaginary
    def str (self):
        if self.re==0 and self.im==0:
           return "0"
        if self.re==0 and self.im>0:
            return "i{}".format(self.im)
        if self.re==0 and self.im<0:
            return "-i{}".format(-self.im)
        if self.im<0:</pre>
            return "{}-i{}".format(self.re, -self.im)
        if self.im>0:
            return "{}+i{}".format(self.re, self.im)
        return str(self.re)
    def length(self):
        return math.sqrt(self.re*self.re+self.im*self.im)
if name == " main ":
    a = Complex(-2, 3)
    print(a.length())
```

```
class Complex():
    def init (self, real, imaginary):
        self.re = real
        self.im = imaginary
    def str (self):
        if self.re==0 and self.im==0:
           return "0"
        if self.re==0 and self.im>0:
            return "i{}".format(self.im)
        if self.re==0 and self.im<0:
            return "-i{}".format(-self.im)
        if self.im<0:
            return "{}-i{}".format(self.re, -self.im)
        if self.im>0:
            return "{}+i{}".format(self.re, self.im)
        return str(self.re)
    def length(self):
        return math.sqrt(self.re*self.re+self.im*self.im)
```

if __name__ == "__main__":
 a = Complex(-2, 3)
 print(a.length())

Here is how this function is called: The object is followed by a period

```
class Complex():
    def init (self, real, imaginary):
        self.re = real
        self.im = imaginary
    def str (self):
        if self.re==0 and self.im==0:
           return "0"
        if self.re==0 and self.im>0:
            return "i{}".format(self.im)
        if self.re==0 and self.im<0:
            return "-i{}".format(-self.im)
        if self.im<0:
            return "{}-i{}".format(self.re, -self.im)
        if self.im>0:
            return "{}+i{}".format(self.re, self.im)
        return str(self.re)
    def length(self):
        return math.sqrt(self.re*self.re+self.im*self.im)
```

So, this method is really a function of one argument, even if it does not look like it.

```
class Complex():
    def init (self, real, imaginary):
        self.re = real
        self.im = imaginary
    def str (self):
        if self.re==0 and self.im==0:
           return "0"
        if self.re==0 and self.im>0:
            return "i{}".format(self.im)
        if self.re==0 and self.im<0:
            return "-i{}".format(-self.im)
        if self.im<0:
            return "{}-i{}".format(self.re, -self.im)
        if self.im>0:
            return "{}+i{}".format(self.re, self.im)
        return str(self.re)
    def length(self):
        return math.sqrt(self.re*self.re+self.im*self.im)
if name == " main ":
                             Here we are referring to an
    a = Complex(-2, 3)
    print(a.length())
                             instance field.
```

Self Test:

Stop the presentation and fire up IDLE

The phase of a complex number is defined by

$$\arg(a+bi) = \begin{cases} \arctan(\frac{b}{a}) & \text{if } a > 0 \\ \arctan(\frac{b}{a}) + \pi & \text{if } a < 0 \text{ and } b \ge 0 \\ \arctan(\frac{b}{a}) - \pi & \text{if } a < 0 \text{ and } b < 0 \\ \frac{\pi}{2} & \text{if } a = 0 \text{ and } b > 0 \\ -\frac{\pi}{2} & \text{if } a = 0 \text{ and } b < 0 \\ \text{undefined} & \text{if } x = 0 \text{ and } b = 0 \end{cases}$$

 Raise a ValueError in the last case, the arctan in the math library is called atan.

```
class Complex():
    def arg(self):
        if self.re == 0 and self.im == 0:
            raise ValueError
        if self.re > 0:
            return math.atan(self.im/self.re)
        if self.re < 0 and self.im >= 0:
            return math.atan(self.im/self.re)+math.pi
        if self.re < 0 and self.im < 0:
            return math.atan(self.im/self.re) - math.pi
        if self.re == 0 and self.im > 0:
            return math.pi/2
        if self.re == 0 and self.im < 0:
            return -math.pi/2
if name == " main ":
    a = Complex(0, 0)
   print(a.arg())
```

- Methods can of course return other objects
 - The conjugate of a complex number is obtained by reflecting around the y-axis

$$\overline{a+bi} = a-bi$$

OOP in Python

```
class Complex():
    def conjugate(self):
        return Complex(self.re, -self.im)

if __name__ == "__main__":
    a = Complex(2, 3)
    print(a.conjugate())
```

OOP

- Python knows "operator overloading"
 - Instead of adding two complex numbers by saying something like c=add(a,b)
 - We can say c=a+b

 Python knows a number of such overloads and associates them by reserving function names

```
class Complex():
    def __add__(self, other):
        return Complex(self.re+other.re, self.im+other.im)

if __name__ == "__main__":
    a = Complex(2, 3)
    b = Complex(3, -5)
    print(a+b)

We need to return a complex number
```

Here we are adding two complex numbers.

Self Test

- Overload the subtraction
 - The reserved method name is __sub__
 - (Two underscores before and after)

Solution

```
class Complex():
    def __sub__(self, other):
        return Complex(self.re-other.re, self.im-other.im)

if __name__ == "__main__":
    a = Complex(2, 3)
    b = Complex(3, -5)
    suma = a+b
    dif = a-b
    print(a, b, suma, dif)
```

OOP in Python

- We can define comparisons via overloading
 - For equality, the reserved method name is __eq__

OOP in Python

- Resolving operators
 - Operator overloading does not have to happen between objects of the same type
 - If there is an expression a==b
 - Python first looks into the class definition of a for an __eq__ method that has second parameter the type of b
 - If that fails, Python then looks into the class definition of b for an __eq_method

OOP

- In fact, there is a default comparison between two objects
 - It is based on *IDENTITY* **NOT** EQUALITY
 - Identity: Two objects are stored at the same location
 - Equality: Two objects have the same fields

```
class Complex():
    def eq (self, other):
        if isinstance(other, Complex):
            return self.re==other.re and self.im==other.im
        return NotImplemented
    def ne (self, other):
        if isinstance (other, Complex):
            return self.re!=other.re or self.im!=other.im
        return NotImplemented
if name == " main ":
   a = Complex(2, 3)
   b = Complex(3, -5)
   print(a==b, a!=b)
   print(a==Complex(2,3), a!=Complex(2,3))
```

We only want to compare two complex numbers

```
class Complex():
    def eq (self, other):
        if isinstance(other, Complex):
            return self.re==other.re and self.im==other.im
        return NotImplemented
    def ne (self, other):
        if isinstance(other, Complex):
            return self.re!=other.re or self.im!=other.im
        return NotImplemented
if name == " main ":
   a = Complex(2, 3)
   b = Complex(3, -5)
   print(a==b, a!=b)
   print (a==Complex (2,3), a!=Complex (2,3))
```

Two complex numbers are equal if they have the same real and imaginary parts

```
class Complex():
    def eq (self, other):
        if isinstance(other, Complex):
            return self.re==other.re and self.im==other.im
        return NotImplemented
    def ne (self, other):
        if isinstance(other, Complex):
            return self.re!=other.re or self.im!=other.im
        return NotImplemented
if name == " main ":
   a = Complex(2, 3)
   b = Complex(3, -5)
   print(a==b, a!=b)
   print (a = Complex(2,3), a! = Complex(2,3))
```

If we compare a complex number with a noncomplex number then we want to return the constant NotImplemented

Classes and Objects

- Classes usually define objects, but they can also used in isolation
 - Assume that you want to use a number of global variables
 - This is dangerous, since you might be reusing the same name
 - Solution: Use a class that contains all these variables

A Globals Class

- We call the class GI short for global
- Store constants as class variables
- Easy to identify in program

```
class Gl:
    gr2gr = 0.06479891
    dr2gr = 1.7718451953125
    oz2gr = 28.349523125
    lb2gr = 453.59237
    st2gr = 6350.29318
```

```
def translate(number, measure):
    if measure == "gr":
        return "{0:.3f} {1}".format(number*Gl.gr2gr, "gram")
    if measure == "dr":
        return "{0:.3f} {1}".format(number*Gl.dr2gr, "gram")
    if measure == "oz":
        return "{0:.3f} {1}".format(number*Gl.oz2gr, "gram")
    if measure == "lb":
        return "{0:.3f} {1}".format(number*Gl.lb2gr, "gram")
    if measure == "st":
        return "{0:.3f} {1}".format(number*Gl.st2gr/1000, "kg")
    raise ValueError
```

Class and Instance Variables

- Class variable
 - belong to the class
 - shared by all objects
 - defined without prefix in the class
- Instance variable
 - belong to the instance
 - not shared by objects
 - defined by using an object or self prefix

Self Test

Identify the type of the bold-faced variables in the following code

```
import math
class Example:
    exists = False
    def init (self, x, y):
        self.radius = math.sqrt(x*x+y+y)
        self.x = x
        self.y = y
        Example.exists = True
print(Example.exists)
e = Example(2, 3)
print(e.x)
print (Example.exists)
print (e.radius)
```

```
class Example:
    exists = False
    def __init__(self, x, y):
        self.radius = math.sqrt(x*x+y+y)
        self.x = x
        self.y = y
        Example.exists = True
```

```
print(Example.exists)
e = Example(2, 3)
print(e.x)
print(Example.exists)
print(e.radius)
```

import math

This is an instance variable. It belongs to the (one and only) object of type Example.

It happens to be defined in __init__. However, it is defined with the self prefix.

```
import math

class Example:
    exists = False
    def __init__(self, x, y):
        self.radius = math.sqrt(x*x+y+y)
        self.x = x
        self.y = y
        Example.exists = True
```

```
print(Example.exists)
e = Example(2, 3)
print(e.x)
print(Example.exists)
print(e.radius)
```

This is a class variable. It is specified by using the class name "Example."

It is defined without a prefix within the class.

```
import math
class Example:
    exists = False
    def init (self, x, y):
        self.radius = math.sqrt(x*x+y+y)
        self.x = x
        self.y = y
        Example.exists = True
print(Example.exists)
e = Example(2, 3)
print(e.x)
```

print(Example.exists)

print (e.radius)

This is an instance variable. It is defined with the prefix self.

It is used by referring to an object e.

Class and Instance Methods

- The same distinction can be made for methods
 - Methods are functions related to an object
- A class method depends only on the class.
 - It is defined in the class, but has no argument self
 - It is called by giving the class-name
- An instance method depends on an instance
 - It is defined in the class with first argument self
 - It is called by prefacing it with an instance.
 - The instance is called the implicit argument

Class and Instance Methods

```
class Example:
    def foo():
        print("foo")
    def __init___(self):
        pass
    def bar(self):
        print("bar")

Example.foo()
e = Example()
e.bar()
```

A method definition without argument self:
Class Method

It is called using the class-name to call it

Class and Instance Methods

```
class Example:
    def foo():
        print("foo")
    def __init___(self):
        pass
    def bar(self):
        print("bar")

Example.foo()
e = Example()
e.bar()
```

A method definition with argument self:
Instance Method

It is called using the Instance.
Without an object e, we cannot call it.

Self Test

Identify the type of methods in the following code

```
import math
class Vector3D:
    def __init_ (self, x, y, z):
        self.x = x
        self.y = y
        self.z = z
    def zeroes():
        return Vector3D(0,0,0)
    def ones():
        return Vector3D(1,1,1)
    def add (self, other):
        return Vector3D(self.x+other.x,
                        self.y+other.y,
                        self.z+other.z)
    def str (self):
        return "({}, {}, {})".format(self.x, self.y, self.z)
    def length(self):
        return math.sqrt(self.x**2+self.y**2+self.z**2)
```

Dunder (double under) method: Hard to tell

```
import math
class Vector3D:
   def init (self, x, y, z):
        self.x = x
        self.y = y
        self.z = z
   def zeroes():
        return Vector3D(0,0,0)
   def ones():
        return Vector3D(1,1,1)
   def add (self, other):
        return Vector3D(self.x+other.x,
                        self.y+other.y,
                        self.z+other.z)
   def str (self):
        return "({}, {}, {})".format(self.x, self.y, self.z)
   def length(self):
        return math.sqrt(self.x**2+self.y**2+self.z**2)
```

```
import math
class Vector3D:
    def init (self, x, y, z):
        self.x = x
                                    Class Method, even though it
        self.y = y
                                    generates an object
        self.z = z
    def zeroes():
        return Vector3D(0,0,0)
    def ones():
        return Vector3D(1,1,1)
    def add (self, other):
        return Vector3D(self.x+other.x,
                        self.y+other.y,
                        self.z+other.z)
    def str (self):
        return "({}, {}, {})".format(self.x, self.y, self.z)
    def length(self):
        return math.sqrt(self.x**2+self.y**2+self.z**2)
```

```
import math
class Vector3D:
    def init (self, x, y, z):
        self.x = x
        self.y = y
        self.z = z
                                    Class Method, even though it
    def zeroes():
                                    generates an object
        return Vector3D(0,0,0)
    def ones():
        return Vector3D(1,1,1)
    def add (self, other):
        return Vector3D(self.x+other.x,
                        self.y+other.y,
                        self.z+other.z)
    def str (self):
        return "({}, {}, {})".format(self.x, self.y, self.z)
    def length(self):
        return math.sqrt(self.x**2+self.y**2+self.z**2)
```

```
import math
class Vector3D:
   def init (self, x, y, z):
        self.x = x
        self.y = y
        self.z = z
   def zeroes():
        return Vector3D(0,0,0)
   def ones():
                                    Instance method
        return Vector3D(1,1,1)
   def add (self, other):
        return Vector3D(self.x+other.x,
                        self.y+other.y,
                        self.z+other.z)
   def str (self):
        return "({}, {}, {})".format(self.x, self.y, self.z)
   def length(self):
        return math.sqrt(self.x**2+self.y**2+self.z**2)
```

```
import math
class Vector3D:
   def init (self, x, y, z):
        self.x = x
        self.y = y
        self.z = z
   def zeroes():
        return Vector3D(0,0,0)
   def ones():
        return Vector3D(1,1,1)
   def add (self, other):
        return Vector3D(self.x+other.x,
                        self.y+other.y,
                                         Dunder instance method
                        self.z+other.z)
   def str (self):
        return "({}, {}, {})".format(self.x, self.y, self.z)
   def length(self):
        return math.sqrt(self.x**2+self.y**2+self.z**2)
```

```
import math
class Vector3D:
   def init (self, x, y, z):
        self.x = x
        self.y = y
        self.z = z
   def zeroes():
        return Vector3D(0,0,0)
   def ones():
        return Vector3D(1,1,1)
   def add (self, other):
        return Vector3D(self.x+other.x,
                        self.y+other.y,
                                           Instance method
                        self.z+other.z)
   def str (self):
        return "({}, {}, {})"..ormat(self.x, self.y, self.z)
   def length(self):
        return math.sqrt(self.x**2+self.y**2+self.z**2)
```

- Python reserves special names for functions that allows the programmer to emulate the behavior of built-in types
 - For example, we can create number like objects that allow for operations such as addition and multiplication
 - These methods have special names that start out with two underscores and end with two underscores

 Aside: If you preface a variable / function / class with a single underscore, you indicate that it should be treated as reserved and not used outside of the module / class

- A class for playing cards:
 - A card has a suit and a rank
 - We define this in the constructor __init__

```
class Card:
    def __init__(self, suit, rank):
        self.suit = suit
        self.rank = rank
```

- We want to print it
 - Python likes to have two methods:
 - __repr__ for more information, e.g. errors
 - __str__ for the print-function
 - Both return a string

```
class Card:
    def __str__(self):
        return self.suit[0:2]+self.rank[0:2]
```

```
def __repr__(self):
    return "{}-{}".format(self.suit, self.rank
```

__repr__ is used when we create an object in the terminal

```
>>> Card("Heart", "Queen")
Heart-Queen
```

_str__ is used within print or when we say str(card)

```
>>> print(Card("Heart", "Queen"))
HeQu
>>> str(Card("Heart", "Queen"))
'HeQu'
```

- We now create a carddeck class
 - Consists of a set of cards
 - Constructor uses a list of ranks and a list of suits

 We create the string method. Remember that it needs to return a string.

- In order to allow python to check whether a deck exists, we want to have a length class. Besides, it is useful in itself.
 - if deck: works by checking len (deck)

```
class Deck:
```

```
def __len__(self):
    return len(self.cards)
```

- Given a deck, we want to be able to access the i-th element.
- We do so by defining __getitem

```
class Deck:
    def __getitem__(self, position):
       return self.cards[position]
```

• This turns out to be very powerful:

We can print out the i-th element of the deck

```
>>> str(french_deck[5])
'Sp9'
```

But we can also slice the deck

```
>>> print(french_deck[6:12])
[Spade-8, Spade-7, Spade-6, Spade-5, Spade-4, Spade-3]
```

We can use random.choice() to select a card

```
>>> random.choice(french_deck)
Diamonds-9
```

 Only for random.sample do we need to go to the underlying instance field

```
>>> random.sample(french_deck.cards, 5)
[Hearts-8, Hearts-2, Hearts-Ace, Hearts-6, Diamonds-Ace]
>>> random.sample(french_deck.cards, 5)
[Hearts-5, Clubs-Queen, Diamonds-Ace, Clubs-3, Clubs-King]
```

 But this is ugly and we better write a class method for it.